## Abstract for a poster

## Block Newton methods for improving groups of singular values

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Consider a rectangular matrix  $A \in \mathbb{R}^{m \times n}$ ,  $m \leq n$ , that has q positive singular values  $\sigma_{i_1}, \ldots, \sigma_{i_q} > 0$  which are separated from the remaining ones but may be clustered or multiple. For simplicity of notation we denote these singular values by  $\sigma_1, \ldots, \sigma_q$  and set  $\Sigma_q := \operatorname{diag}(\sigma_1, \ldots, \sigma_q)$ , and let im  $U_q =$  $\operatorname{span}\{u^1, \ldots, u^q\}$ , im  $V_q = \operatorname{span}\{v^1, \ldots, v^q\}$  be the corresponding left and right singular subspaces, resp., i.e., we have  $A V_q = U_q \Sigma_q$ ,  $A^T U_q = V_q \Sigma_q^T$ . We are interested in improving approximations im  $X \approx \operatorname{im} U_q$ , im  $Y \approx \operatorname{im} V_q$ defined by matrices  $X \in \mathbb{R}^{m \times q}$ ,  $Y \in \mathbb{R}^{n \times q}$  with  $X^T X + Y^T Y = I_q$  and  $X^T A Y + Y^T A^T X = S = \operatorname{diag}(s_1, \ldots, s_q)$  by a rapidly convergent method. The last property can be achieved by a Rayleigh-Ritz step of dimension q. For doing so we apply the quadratically convergent, generalized Rayleigh-Ritz procedure proposed by Lösche, Schwetlick, and Timmermann to the symmetric matrix  $C = \begin{bmatrix} 0 & A \\ A^T & 0 \end{bmatrix}$ . This requires per step to solve q bordered linear systems with matrices

$$\begin{bmatrix} -s_i I & A & X \\ A^T & -s_i I & Y \\ X^T & Y^T & 0 \end{bmatrix} \in \mathbb{R}^{(m+n+q)\times(m+n+q)}, \quad i = 1, \dots, q,$$

followed by a q-dimensional Rayleigh-Ritz process.